DOCUMENT RESUMB

ED 117 570

CE 006 287

AUTHOR TITLE

Nuschler, Alexandra; And Others

General Mathematics; Part 1. Mathematics Curriculum

Guide (Career Oriented) .

· Insaitution REPORT NO

Louisiana State Dept. of Education, Baton Rouge.

Bull-1270: VT-102-466

May 74

PUB DATE note 4

63p.; For related documents, see CE And 282-291; The

table of contents is incomplete

EDRS PRICE & DESCRIPTORS

MF-\$0.83° HC-\$3.50 Blus Postage

Arithmetic; Behavioral Objectives; *Career Education;

Continuous Progress Plan; *Curriculum Guides; Geometry; Learning Activities; *Mathematics; Mathematics Curriculum; Measurement; *Secondary

Education: Statistics

IDENTIFIERS

Louisiana

ABSTRACT

The curriculum guide for secondary level, career-oriented General Mathematics Part 1, correlates performance objectives in basic mathematics with career-oriented concepts and activities. The material is designed to lead the student in a systematic Aevelopment that provides for continuous progress The guide is in outline format, providing a curriculum outline, performance objectives, and related (career-oriented) concepts. objectives, and learning activities. The guide encompasses the main topic areas of developmental arithmetic, introduction to algebra, 🥒 geometry, measurement, introduction to statistics, and enrichment topics. (NJ)

Documents acquired by ERIC include many informal unpublished

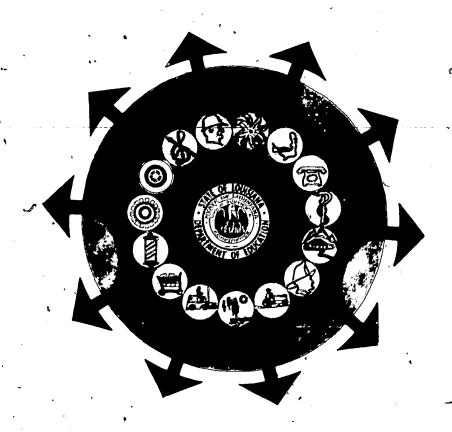
materials not available from other sources. ERIC makes every effort to obtain the best copy available. Nevertheless, items of marginal

reproducibility are often encountered and this affects the quality

of the microfiche and hardcopy reproductions ERIC makes available

via the ERIC Document Reproduction Service (EDRS). EDRS is not responsible for the quality of the original document. Reproductions

supplied by EDRS are the best that can be made from the original.



MATHEMATICS CURRICULUM GUIDE CAREER ORIENTED GENERAL MATHEMATICS PART 1

Louis J. Michot, Superintendent

1974

BULLETIN NO. 1270.

US DEPARTMENT OF HEALTH EDUCATION & WELFARE NATIONAL INSTITUTE OF EDUCATION

THIS DOCUMENT HAS BEEN REPRO DUCED EXACTLY AS RECEIVED FROM THE PERSON OR ORGANIZATION ORIGIN ATING IT POINTS OF VIEW OR OPINIONS STATED DO NOT NECESSARILY REPRE SENT OFFICIAL NATIONAL INSTITUTE OF EDUCATION POSITION OR POLICY ATHEMATICS CURRICULUM GUIDE

(CAREER ORIENTED)

GENERAL MATHEMATICS

PART I

LOUISIANA STATE DEPARTMENT OF EDUCATION

Louis J. Michot

State Superintendent

May 1974

ACKNOW LEDGEMENTS

Appreciation is expressed to the original writing team which worked so diligently in developing the materials and ideas included in the guideline.

Mrs. Alexandra Nuschler, Chairwoman

Chalmette High School Chalmette, Louisiana

Mrs. Eleanor Hollingsworth

Logiawn Junior High Monroe, Louisiana

Mrs. Jocelyn Landry

Coteau-Bayou Blue Elementary Houma, Louisiana

Mr. John H. Smith

Rayville High School Rayville, Louisiana

Mrs. Margaret Thames

Mangham Junior High Mangham, Louisiana

For their constructive suggestions and additions in this revised edition, we give special thanks and acknowledgement to this year's team.

Dr. Merlin M. Ohmer, Chairman

Nicholls State University Thibodaux, Louisiana

Mr. Dale Fredrick

Lafayette Parish School Board Lafayette, Louisiana

Mr. Dale Hester

Nicholls State University Thibodaux, Louisiana

Mr. Joseph Jones

Mansfield High School Mansfield, Louisiana

Mrs. Alexandra Nuschler

Chalmette High School Chalmette, Louisiana

Mrs. Marguerite Sanders

Sabine Parish School Board Many, Louisiana

Finally, we express our gratitude to Superintendent Louis J. Michot, who has been the spearhead in promoting the concept of career education for all, and to the Louisiana Legislature which recognized the need for such a program and saw that funds were made available to carry on this worthwhile endeavor.

PREFACE

The first working draft of the Mathematics Curriculum Guide,
Secondary Level was distributed for field testing for the 1973-74
academic year. Feedback indicated that the materials were appropriate
for the purposes as stated in the original preface.

The imaterials presented herein have been changed from the original only in that the mathematical language has been made as uniform as possible for clarity and to conform to the texts adopted by the State of Louisiana. Additional career learning activities have been introduced.

The format has been revised so that it should be easier to correlate the curriculum outlines and performance objectives with the related career officented concepts and learning activities.

The reader who is seeing the materials for the first time can be assured that the career approach of these guidelines in no way weakens the present program. As in all good educational procedures, materials are included so that all levels may be served. In addition to the ambitious minimum recommendations the guidelines contain ample extension materials for those students who need to be challenged.

Mathematics is embedded in all of the disciplines and makes a solid base for experiences in career education. This is borne out by the numerous references and career activities from the spectrum of life.

The student is led in a systematic development that is designed to provide for continuous progress. Dignity of the person was always foremost in devising and revising the guidelines. The goals were set to give maximum development of the individual through all types of educational experiences.

Finally, our schools will always have a basic curriculum. The methods of instruction will be constantly changing, and the counselors will continue to lend their influence in guiding the putil. The career education goals which are interwoven with the traditional will help make more productive citizens of Louisiana's most important assets, its children.



iii

TABLE OF CONTENTS

•			Pag
Acknowledgement			ii
Preface			iįi
Developmental Arithmetic	•		Ķ
Meaning and Illustration of Set	ខ		1
Counting			3
Expanded Notation and Place V	alue ,		5
Addition of Whole Numbers	s	•	. 5
Subtraction			· 7
Multiplication			7
Division		•	<i>E</i> 9
Whole Numbers and Their Fac	tors		, 11
Fractional Numbers	-		•13
Ratio, Proportion, and Percen	nt		17
Problem Solving	• •		. 19
Introduction to Algebra			21
Symbols, Terminology and Oro	der of Operations		. 21
Properties of Numbers			23
Monomials and Polynomials		•	23
Equations and Inequalities		•	25°
Geometry		•	29
Definitions and Identification	•		29

GENERAL MATHEMATICS PART I

44

ERIC Full Text Provided by ERIC

CURR	TOIT	T TILY	OTTE	TRIE
CURR	H. H.	LALIM		JIN P.

PERFORMANCE, OBJECTIVES

I. Developmental Arithmetic

- A. Meaning and illustrations of sets
 - Kinds of sets
 a. Finite set
 b. Infinite set
 - 2. Identify elements
 - a. Ruleb. Roster
 - 3. Subset of a set
 - 4. Comparison of two sets

5. Definition and identification

- I. Developmental Arithmetic
 - A. To demonstrate a basic understanding of sets, the student should be able to:
 - Define and illustrate:
 a. Finite set.
 - b. Infinite set.
 - 2. Specify the elements of given sets by:a. Rule.b. Roster.
 - 3. List the subsets of the given set A, such as A = {1, 2, 3, 4}.
 - 4. Compare two given sets A and B by using the correct relation(s).
 - a. n(A) = n(B).
 - b. $n(A) \neq n(B)$.
 - c. n(A) > n(B).
 - d. n(A) < n(B).
 - 5. Give a problem similar to the following: U = {a, b, c, d, e, f};
 A = {a, b, c,}; B = {c, d, e}; C = {f}.

 Draw a Venn diagram to illustrate each of the following sets:

RELATED CAREER ORIENTED LEARNING ACTIVITIES

I. Career Concept

Different careers are interrelated.

Performance Objectives

- A. People in all walks of life use sets.
- A. The mechanic uses a set of wrenches; the draftsman uses a set of drafting instruments to draw plans of structures or machines; the homemaker uses a set of dishes. On 3 × 5 cards list jobs and careers from the different job clusters. On other cards list sets of things that are used in the jobs or careers. Have the student match the job cards to the correct sets.

PERFORMANCE OBJECTIVES

- a. Universal set,
- b. Empty set,
- c, Union of sets
- d. Intersetion of sets
- e. Disjoint sets
- f. Complement of a set
- B. Counting
 - 1. By 2's
 - 2. By 5's
 - 3. By 10's
 - 4. Distinction between odd and even numbers
 - 5. Halves
 - 6. Thirds
 - 7. Yourths
 - 8. Tenths

- a. AOB
- b. A U B.
- c. A C; A and C are called sets: A C is the set.
- the d. A.
- B. To demonstrate a basic understanding of counting, the student should be able to:
 - 1. Count to 100 by 2's.
 - 2. Count to 100 by 5's.
 - 3. Count to 1,000 by 10's.
 - 4. Select from a given list of numbers:
 - a. Odd numbers.
 - b. Even numbers.
 - 5. Count by:
 - a. Halves.
 - b. Thirds.
 - c. Fourths.
 - d. Tenths.

B. A cashier in a bank uses a basic know-ledge of counting.

B. The cashier counts money to people making a withdrawal usually by the denominations of the bills. e.g.; 5's, 10's, and 20's. Have students play the games Monopoly or Life. The cashier should be able to count currency correctly at the proper times. If desired the cashier may be changed while the game is in progress so that other students may have the opportunity to count different denominations of currency.

PERFORMANCE OBJECTIVES

- C. Expanded notation and place value.
 - 1. Expanded notation
 - 2. Reading of whole numbers
- D. Addition of whole a numbers
 - Identification and application of properties

- 2. Basic addition facts
- 3. Application of expanded notation

- C. To demonstrate a basic understanding of expanded notation and place value, the student should be able to:
 - 1. Write a two-digit number in expanded notation.
 - 2. Read numbers not exceeding one billion.
- D. To demonstrate a basic understanding of addition, the student should be able to:
 - 1. Identify and apply:
 - a. The closure property for addition.
 - b. The commutative property for addition.
 - c. The associative preserty for addition.
 - d. The identity property for addition.
 - e. The cancellation property for addition.
 - 2. State the basic addition facts.
 - 3. Apply expanded notation to:

RELATED CAREER ORIENTED LEARNING ACTIVITIES

C. Radio and television announcers read large. numbers over the air for news stories as bell as for election returns.

D. Department managers within factories use

addition daily in their

C. Collect newspaper articles that have large numbers within the story. Students will read the articles as news announcers.

At local and state election times, collect articles that include election returns. Collect the election returns from the teletype machine of a radio station, television station or newspaper office. Have students read the results as newscasters.

Henry's department checks D. parts for a bicycle factory, sorting them as acceptable or as rejects. On Monday, they found 493 acceptable parts and 2 rejects; on Tuesday, 561 acceptable and 4 rejects; on Wednesday, 389 acceptable and 9 rejects; on Thursday, 461 acceptable and 6 rejects; and on Friday, 533 acceptable and no rejects. How many acceptable parts did they find for the week? How many ' rejects?

Arnold played 18 holes of golf with the score on each hole as follows:

First nine

Hole no. 1 2 3 4 5 6 7 8 9
Par 4 4 3 5 4 4 4 5 3
Arnold 5 7 4 4 5 5 4 7 3



PERFORMANCE OBJECTIVES

- a. Adding two-digit numbers.
- b. Adding three-digit numbers.
- c. Adding columns of numbers.

E: ·Subtraction

- 1. Inverse of addition
- 2. Basic subtraction facts.
- 3. Subtraction without regrouping
- 4. Application of expanded notation
- F. Multiplication
 - Identification and application of properties

- E. In order to demonstrate a basic understanding of subtraction, the student should be able to:
 - Identify and apply subtraction as the inverse of addition.
 - 2. State the basic subtraction facts.
 - 3. Subtract without regrouping.
 - 4. Apply expanded notation to:
 - a. The subtraction of two-digit numbers.
 - b, The subtraction of head three-digit numbers.
- F. In order to demonstrate a basic understanding of multiplication, the student should be able to:
 - 1. Identify and apply:
 - a. The closure property for multiplication.
 - The commutative property for multiplication.

RELATED CAREER ORIENTED LEARNING ACTIVITIES

Second nine

Hole no. 10 11 12 13 14 15 16 17 18

Par 4 5 4 4 3 4 5 4 3

Arnold 6 5 5 5 2 5 6 4 3

What was Arnold's score for the first nine holes? What was his score for the eighteen holes? What is par for the first nine and for the eighteen holes?

E. Salesmen for wholesale companies must travel to many different 'towns. They use subtraction in determining the shortest routes to travel.

E. John Stoner calculated the distance from Chicago to Miami by one route to be 1374 miles, by a second route to be 1445 miles, and by a third route to be 1423 miles. How many miles more must he travel if he chooses the third route instead of the shortest route?

F. The farmer uses multiplication of whole numbers.

F. The farmer has 1,000 head of steers in a feed lot. The average weight per steer is 700 pounds. The water requirement for a 700 pound steer is 12 gallons per day. How many gallons of water will be required to water the 1000 steers each day? How much water will be required in a month?

PERFORMANCE OBJECTIVES



property for multi-, plication.
d. The identity propert

The associative

- d. The identity property for multiplication.
- e. The inverse property for multiplication.
- f. The distributive ., property for multiplication over addition.
- g. The multiplication property of zero.
- h. The cancellation property for multiplication.
- 2. Express the multiplication of whole numbers as repeated addition.
- 3. State the multiplication facts through 12×12 .
- G. In order to demonstrate a basic understanding of division, the student should be able to:
 - 1. Divide by means of repeated subtraction, e.g., $24 \div 6 = 4$. because: 24 6 = 18; 18 6 = 12; 12 6 = 6; 6 6 = 0.
 - 2. Identify and apply division as the inverse of multiplication.

2., Repeated addition

3. Statement of facts through 12 × 12

G. Division

1. Repeated subtraction

2. Inverse of multiplication

RELATED CAREER ORIENTED LEARNING ACTIVITIES

G. The production manager G. uses division of whole numbers in his work.

The production manager reports that 1815 pounds of cereal were manufactured on Monday; 2145 pounds on Tuesday; 1980 pounds on Wednesday; 2310 pounds on Thursday, and 1650 pounds on Friday. The cereal was packaged in 11 ounce packages. How many packages of cereal were produced each day? How many for the week? If the company had used 15 ounce packages, how many packages would be produced for the week?

PERFORMANCE . OBJECTIVES

- 3. Division by a onedigit number
- 3. \(\) Divide a multi-digit number by a onedigit number; e.g., $24 \div 6 = 24 \times \frac{1}{6} = 4.$

4. Division by twodigit and threedigit divisors

- 4. Divide by a two-digit or three-digit divisor.
- 5. Checking by multiplication
- 5. Check division by multiplication.

6. Impossibility of division by zero

6. Explain why division by zero is impossible (using repeated subtraction).

- H. Whole numbers and their factors
- H. In order to demonstrate a basic understanding of whole numbers and their factors, the student should be able to:

l. Multiples

l. List five multiples of a given number.

2. Factors

2. List the set of all factors of a given number.

3. Primes and composites

3. From a given set of numbers, identify:
a. Primes.
b. Composites.

4. Unique factorization theorem

4. Express a given number as a product of its prime factors.

5. Least common multiple

5. Determine the least common multiple of two given numbers.

- Greatest common factors
- 6. Determine the greatest common factor of two given numbers.

RELATED CAREER ORIENTED LEARNING ACTIVITIES

Solution:

	lloz.	15 oz.
Monday	2640	1936
Tuesday	3120	2288
Wednesday	2880	2112
Thursday	3360	2464
Friday	2400	176Ø
Total	14,400	10,560

H. Athletes use factors in different ways in oral communication.

H. Milton, John, and Jim are preparing for the olympics.

I ran two mixes each day for ten days.

I took a four mile run five times.

Milton

I went on a two-mile run twice a day for five days.

Write the expressions to show the number of miles that Milton, John, and Jim walked.

Jim

 2×10 4×5 $2 \times 2 \times 5$

What number does each expression name? Which expression is written with only prime factors?



- I. Fractional numbers
 - 1. Fractions
 - a. Numerator and denominator
 - b. Reading and writing fractions
 - c. Equivalent
 - d. Comparison

- e. Addition
- f. Subtraction
- g. Multiplication

- I. Fractional numbers
 - 1. To demonstrate a basic understanding of fractions, the student should be able to:
 - a. Identify the numerator and the denominator of the fraction a.
 b
 - b. Read and write fractions.
 - c. List the equivalent fractions from a given set of fractions.
 - d. Use the symbols = ,
 >, <, to compare
 fractions like the
 following:</pre>

$$\frac{5}{8}$$
 0 $\frac{3}{4}$; $\frac{1}{2}$ 0 $\frac{5}{10}$

$$\frac{2}{3}$$
 \bigcirc $\frac{5}{9}$

- e. Add two or more fractions:
 - (1) With equal denominators.
 - (2) With unequal denominators.
- f. Subtract fractions:
 - (1) With equal denominators.
 - (2) With unequal denominators.
- , g. Multiply two or more fractions.

Ø

RELATED CAREER ORIENTED LEARNING ACTIVITIES

I. Compilers of the yearly United States Almanac use fractional numbers.

Lumber salespeople use fractional numbers in denoting thickness of boards.

In America 4/5 of our population lives in cities that occupy 1/50 of our land. If the area of the United States is approximately 2,800,000 square miles and our population is approximately 205 million people, how many people live in cities? How many square miles of land do they occupy?

Answer: 164,000,000 people 56,000 square miles

Example: Lumber yards sell boards 5/4" in thickness and refer to them as 5-quarter boards. What would be the total thickness of 6 five-quarter boards?

1



PERFORMANCE OBJECTIVES

- h. Division
- 2. Decimals
 - a. Notation
 - b. Rounding

- c. Repeating and terminating
- d. Addition

e. Subtraction

(;

- h. Divide a fraction by a fraction.
- 2. To demonstrate a basic understanding of decimals, the student should be able to:
 - a. Read and write decimals.
 - b. Round a given decimal such as 2,601,000.32756 to:
 - (1) Thousandths.
 - , (2) Hundredths.
 - (3) Tenths.
 - (4) Thousands.
 - (5) Millions.
 - c. Define and give an example of a:
 - (1) Repeating decimal.
 - (2) Terminating decimal.
 - d. Compute the sum of two or more given decimals:
 - (1) With the same ... number of decimal places.
 - (2) With different numbers of decimal places.
 - e. Compute the difference of two decimals.



RELATED CAREER ORIENTED LEARNING ACTIVITIES

Weathermen, carpenters, nurses, physicians, dentist, ... bankers, store clefks, and many others 'must be able to read and compute with decimals. Learning activities that involve how some of these use decimals are left to the initiative of the individual teacher.

Reconcile the following bank balance. For one month the balancg in the checkbook at the end of the month was \$689.58. The balance of the bank statement was \$483.50. A deposit of \$302.10 was in transit. The checks outstanding for the month before were #86 (\$48.12), #89 (\$9.56), # 90 (\$32.17), and #91 (\$25.03). These checks were written in the present month: #92 (\$105.00, #93 (\$14.27), · #94 (\$31.15), #95 (\$40.00), #96 (\$8.53), #97 <u>(</u>\$\frac{1}8.29), #98 (\$26.25), #99 (\$50.00), and #100 (\$15.50). These checks were paid by the bank. during the present month: #86, #89, #90, #91, #92, #94, #96, and #97. There was a bank debit memo for \$10.00 for the rent of his safe deposit box for one year.



PERFORMANCE OBJECTIVES

- f. Multiplication
- g. Division
- 3, Conversion of:
 - a. Decimal form to fractional form
 - b. Fractional form to decimal? form
- J. Ratio, Proportion, and Percent
 - l. Ratio

-d

- a. Definition
- b. Writing ratios
- 2. Proportion
 - a. Definition
 - b. Means and extremes
 - c. Problem solving
- 3. Percent
 - a. Definition
 - b. Ratio-percent relationship
 - c. Problem solving

- f. Compute the product of two decimals.
- g. Divide a decimal by a decimal.
- 3. To demonstrate a basic understanding of converting, the student should be able to:
 - a. Convert given decimals to fractions.
 - b. Convert given fractions to decimals.
- J. To demonstrate an understanding of ratio, proportion, and percent, the student should be able to:
 - 1. Express in two notations the ratio of boys in the class to girls in the class.
 - 2. Solve problems by using proportion.
 - 3. Express a given percent as a fraction and as a decimal.

J. A pollster uses ratio and proportion in analyzing data.
 Results of polls are often expressed as percents.

The credit manager of a bank uses percent.

Salespeople should be able to solve problems involving their earnings paid on a commission basis.

J. In a survey of 1,000 voters just before an election, a pollster found that 750 people intended to vote for candidate A and 250 intended to vote for candidate B. What was the ratio of those in favor of A to the total number of votes included in the poll?

What was the ratio of the number in favor of B to the toal number of voters included in the poll?

What percent of the total votes could candidate A expect?

Soltuion: 3:4 1:4 75%

Compute the commissions earned by these salespeople. These are the various commission plans.

Plan I: No quota. Commission is paid on all sales.

Plan II: Commission is paid only on sales over the quota.

Plan III: Commission is paid on all sales if the quota is made.

•

Problem Solving

K.

- 4. Solve problems computing:
 - a. Percent one number is of another number.
 - b. Percent of a number.
 - c. A number when the precent (rate) and the percentage are known.
- K. In to demonstrate a basic understanding of problem solving, the student should be able to solve simple one-step and two-step problems.



-RELATED CAREER ORIENTED LEARNING ACTIVITIES

•	\ .			
Salesperson	Sales	Quota	Rate	Plan
Flora	`\$625 . 34	None	3%	I
Rex	740.35	\$550	4%	III
Marshall	699.36	450	4%	ŢII
Sandra	451.02	None	3%	I
Chauncey	928.59	600	4%	II
Harold	874, 27	500	3%	ш
Neal	957. 36	550°	3%	II
Yolanda	416.84	550	3%.	II

K. Astronauts must solve problems encountered in space exploration.

A contractor must solve problems to determine the cost of remodeling or building. K. On July 20, 1969, astronaut
Neil Armstrong landed on the
moon in a Lunar Module. He
walked on the lunar surface for
.0972 of an earth day. Calculate this in hours and
minutes (approximately).

Mr. Brown, a contractor, was asked to submit a bid price on remodeling a kitchen. He had to include 2 new cabinets

@ \$350.00 each, a built-in oven @\$245.50, a cook top

@ \$150.00, a dishwasher

@\$185.00, and a new sink

@ \$60.00. The labor for removing the old appliances and cabinets, and installing the new ones would be \$1,000. He desires a profit of 10 percent of his total cost. What should his bid price be?

PERFORMANCE OBJECTIVES

II. Introduction to Algebra

II. Introduction to Algebra

- A. Symbols, terminology, and order of operations
 - 1. Identification of symbols
 - 2. Definition and illustration

- A. To develop a basic understanding of symbols, terminology, and order of operations, the student should be able to:
 - l. Identify mathematical symbols: =, \neq , >, <, +, -, \times , ., \div , \times , (), [].
 - 2. Define or illustrate:
 - a. Positive number (on the number line).
 - b. Negative number (on the number line).
 - c. Equation.
 - d. Inequality.
 - e. Absolute value.
 - f. Variable.
 - g. Coefficient.
 - h. Constant.
 - i. Integer.
 - j. Additive identity.
 - k. Additive inverse of a given number.
 - l. Multiplicative identity.
 - m. Multiplicative inverse (reciprocal).

RELATED CAREER ORIENTED LEARNING ACTIVITIES

II. Career Concept

Individuals have different abilities, interests, needs, and values.

Performance Objectives

A. A school cafeteria manager uses positive and negative numbers to determine daily income and expenses.

- A. Positive numbers are often used to indicate income and negative numbers to indicate expense.

 Study these receipts and purchases of a school cafeteria:
 - 1. Bread purchase, \$4.40
 - 2. Soda receipts for student government meeting, \$3.50.
 - 3. Doughnut receipts, \$1.10.
 - 4. Milk purchase, \$2.00.
 - 5. Purchase of rolls, \$2.75.
 - 6. Purchase of lunch meat, \$3.75.
 - 7. Receipts from teacher's lunches, \$28.30.
 - 8. Purchase of ice cream, \$4.80.
 - 9. Coffee receipts for teacher's lounge, \$5.60.

Identify each item as either income or expense. Label as positive the numerals for income, and as negative, the numerals for expenses. Compute both the total income and the total expense. Compute the profit or loss.

PERFORMANCE OBJECTIVES

- B. Properties of numbers
 - 1. Closure
 - a. Addition
 - b. Multiplication
 - 2. Commutative
 - a. Addition
 - b. Multiplication
 - 3. Associative
 - a. Addition
 - b. Multiplication
 - 4. Identity
 - a. Addition
 - b. Multiplication
 - 5. Inverse .
 - a. Addition
 - b. Multiplication
 - 6. Distributive (for multiplication over addition)
- C. Monomials and Polynomials

- B. To demonstrate a basic understanding of the properties of numbers, the student should be able to express, recognize, and use:
 - 1. The closure property for:
 - a. Addition.
 - b. Multiplication.
 - 2. The commutative property <u>for</u>:
 - a. Addition.
 - b. Multiplication.
 - 3. The associative property for:
 - a. Addition.
 - b. Multiplication.
 - 4. The identity property for:
 - a. Addition.
 - b. Multiplication.
 - 5. The inverse property for:
 - a. Addition.
 - b. Multiplication.
 - 6. The distributive property for multi'plication over addition.
- C. To demonstrate a basic understanding of monomials and polynomials, the student should be able to:

RELATED CAREER ORIENTED LEARNING ACTIVITIES

- B. Everybody uses all of the properties of numbers in his daily activities. In particular, the computer programmer uses the distributive property to save steps in computing.

 This results in reduced computer time and cost.
- B. A bookstore sells paper at 18¢ a pack. On Monday 35 packs were sold, and on Tuesday 28 packs were sold. Write the number sentence for the money paid, using the distributive property.

- C. A mathematician uses algebraic expressions to rewrite word expressions.
- C. Study each word expression.
 Write an algebraic expression for each.



PERFORMANCE OBJECTIVES

- 1. Identification and definitions
- Writing in descending powers
- 3. Addition
- 4. Subtraction
- 5. Multiplication
- 6. Division
- 7. Writing polynomial expressions
- D. Equations and inequalities
 - 1. Translation of English statements into algebraic sentences

- l. Identify monomial, binomial, and other polynomials.
- 2. Write polynomials in descending powers; e.g., $y^2 + 4 + 8y^3 + y = 8y^3 + y^2 + y + 4$.
- 3. Add polynomials.
- 4. Subtract polynomials.
- 5. Use the law of exponents to multiply a polynomial by a monomial.
- 6. Use the law of exponents to divide a polynomial by a monomial.
- 7. Translate a given
 English expression to
 a polynomial.
- D. To demonstrate a basic understanding of equations and inequalities, the student should be able to:
 - 1. Translate English statements into algebraic
 sentinces; e.g., "5
 more than the product
 of 3 and a given number
 is 1 translates to
 "3x + 5 = 17".

RELATED CAREER ORIENTED LEARNING ACTIVITIES

- 1. Add 7 to 3 times a given number.
- 2. Add 3 times a given number to 7. (Compare #1 and #2)
- 3. Subtract 7 from 3 times a given number.
- 4. Subtract 3 times a given number from 7. (compare #3 and #4)
- 5. Divide a given number by 3,
- add 4 to the result.
- 6. Add a given number to 3; divide the result by 4.
- 7. Add 6 to 3/5 of a given number.
- 8. The number of cents in 2 dimes and 3 nickels.
- 9. The cost of n stamps at 10¢ each.
- 10. 3 + a given number x, plus twice the square of x, minus 8 times the cube of x, divided by 16.
- D. Engineers and scientists use equations and inequalities in the design of industrial equipment.

D. The designer of a space vehicle has determined the length must not exceed 100 meters, other design requirements determine that main body should be 9 times as long as the nose cone. What is the maximum length of the main body?

Solution: $n + 9n \le 100$.

PERFORMANCE OBJECTIVES

2.

- 2. Translation of algebraic sentences into English statements.
- area of a circle is equal to notimes the square of the radius. "(2r)² means the square of twice a number, a number multiplied by 2 and the product squared or the square of the product of 2 and a number.

Translate algebraic

sentences into English

statements; e.g., "A= π r²" translates to "the

- 3. Evaluating algebraic expressions
- 3. Evaluate expressions such as 3x + 2b if x = 4 and b = -7.

4. Solving open sentences

- 4. Solve open sentences which involves:
 - a. Equations.
 - b. Inequalities.

RELATED CAREER ORIENTED LEARNING ACTIVITIES



PERFORMANCE OBJECTIVES

III. Geometry

III. Geometry ."

- A. Definitions and identification
 - Point, line, planes space
 - 2. Segment and ray
 - 3. Intersecting lines
 - 4. Non-intersecting lines.
 - a. Parallel lines
 - b. Skew lines
 - 5. Definitions of angle
 - a. Right
 - b. Obtuse
 - c. Acute
 - d. Complementary
 - e. Supplementary
 - 6. Perpendicular lines

- A. To demonstrate a basic understanding of geometry the student should be able to:
 - 1. Identify and name point, line, plane, and space.
 - 2. Define and identify segment and ray.
 - 3. Sketch two intersecting lines.
 - 4. Illustrate:
 - a. Parallel lines.
 - b. Skew lines.
 - 5. Define angle.
 - a. Right angle.
 - b. Obtuse angle.
 - c. Acute angle.
 - d. Complementary angle.
 - e. Supplementary angle.
 - 6. From several given diagrams identify perpendicular lines.

RELATED CAREER ORIENTED LEARNING ACTIVITIES

III. Career Concept

Different careers are interrelated.

Performance Objectives

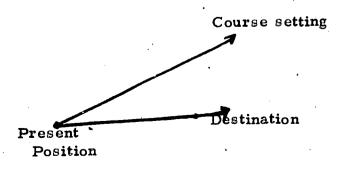
A. Basic geometry is an integral part of navigation. Geometrical models are frequently used by air navigators as well as sailing navigators.

A. If a sailing navigator wants to travel to a certain island and he knows the position of that island relative to his present position, then he sets a compass course heading in the direction of that island. The geometrical model for the compass course to be followed is a ray with endpoint at the present position and the destination as a point on the ray.

Destination

Present Position

If wind (or current) drift is a factor to be considered, then, in order to allow for the drift, the course setting will differ from the direction of the true destination. The geometrical model would be an angle with vertex at the present position, one ray containing the destination as a point and the second ray containing the course setting.





- 7. Simple closed curves
 - a. Polygons
 - (1) Triangles
 - (2) Quadrilaterals of all types
 - (3) Other polygons
 - b. Circles
- 8. Closed space figures
 - a. d Cubes and other prisms
 - b. Pyramids
 - c. Cones
 - d. Cylinders
 - e. Spheres
- B. Perimeter and circumference

- 7. From given diagrams identify the simple closed curves.
 - a. Define and identify polygons.
 - (1) Triangles-equilateral,
 isosceles, right,
 similar, scalene,
 acute, obtuse.
 - (2) Quadrilaterals -rectangle,
 square, para -llelogram, rhombus, trapezoid.
 - (3) Pentagons, hexagons, octagons.
 - b. Identify and/or define circle, center, radius, diameter, chord, arc, central angle, circumference.
- 8. From given diagrams identify:
 - a. Cubes and other prisms.
 - b. Pyramids.
 - c. Cones.
 - d. Cylinders
 - e. Spheres.
- B. To demonstrate an understanding of perimeter and circumference, the student should be able to:

RELATED CAREER ORIENTED LEARNING ACTIVITIES

The architect uses a basic knowledge of polygons in creating new designs for building and other construction.

A woodcraft designer uses the basic understanding of polyhedra in his work.

B. A sheet metal worker must have a working knowledge of perimeter in his layout work.

Use a compass in setting a course of travel from the classroom to a designated area such as the school library or the principal's office.

Give some examples of triangles being used to secure rigid construction through bracings or props. Examine a bridge, or a picture of a bridge, to see how the polygon enters into the construction. Make a sketch to show where polygons are used.

Examine some pictures of Greek or Roman architecture, for examples of polygons or any polygon used for ornamental purposes, rather than construction purposes.

Collect information from the local hoppy shops showing the different shapes of the wooden objects.

Identify each figure as a rectangular solid, cube, pyramid, cylinder, sphere, or cone.

Collect pictures from magazines, catalogs, and newspaper advertisements to identify the many different polyhedra.

B. Leon Thomas called a sheet metal shop to purchase skirting for his mobil home. The owner asked for the dimensions of the mobil home, and told Mr. Thomas that skirting of the correct height would cost \$1.25 per running foot. If the home was 14'×70', what would the skirting cost?

- Definitions of circumference
- perimeter and
- Calculations 2.

- Area of a region
 - Rectangle
 - 2. Square
 - 3. Triangle
 - Circle 4.
- D. Surface area
 - Cube
 - Rectangular prism

- Define perimeter and circumference.
- Compute the perimeter or, circumference of:
 - a. A square.
 - b. A rectangle:
 - c. Any other quadrilateral.
 - d. A circle.
- To demonstrate an understanding of area, the student should be able to compute the area of:
 - A rectangle.
 - A square.
 - A triangle.
 - A circle.
- To demonstrate a basic understanding of surface areas, the student should be able to calculate the surface area of:
 - A cubė.
 - A rectangular prism.



RELATED CAREER ORIENTED LEARNING ACTIVITIES

If the labor for installing the skirting was to be \$75, what would the total cost of the job be?

People in construction, in carpeting or tiling floors, and in many other businesses, need to know how to compute areas.

- D. The construction industry involves many
 careers that require
 computation of surface
 areas of cubes and
 other rectangular
 prisms.
- C. Floor covering is needed for a drive-in hamburger place built in the shape of a circle. If the inside measurement of the building was 28 ft. in diameter, approximately how many square feet of floor covering would be needed? At 48¢ per square foot, installed, what would be the cost of the floor covering? The teacher should provide other learning activities.
- D. John and his father planned to buy material to build a trophy case. The case was to be 12 ft. long, 4 ft high, and one ft. wide. The front, top, and two ends of the case were to be glass. Compute the number of square feet of glass needed? Compute the number of square feet of plywood needed for the back and bottom of the case? If the plywood that they wanted is sold only in sheets 4 ft. by 8 ft., how many sheets of plywood would they have to buy? (Do not consider shelving).

PERFORMANCE OBJECTIVES

- E. Volume of a right circular cylinder and volume of a right prism
- E. To demonstrate a basic understanding of volumes, the student should be able to find the volume of:
 - l. A right circular cylinder.
 - 2. A right prism.

F. Construction

- F. To demonstrate a basic understanding of construction, the student should be able to:
- 1. Line segments

l. Construct line segment equal to a given line segment.

2. Perpendiculars

- 2. Construct a perpendicular:
 - a. Bisector of a line segment.
 - b. To a line at a given point on the line.
 - c. To a line from a point not on the line.

3. Angle bisector

 Construct the bisector of a given angle (acute; right; obtuse).

4. Parallels

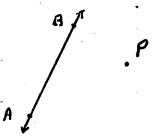
4. Through a point not on a given line, construct the parallel to the given line.

RELATED CAREER ORIENTED LEARNING ACTIVITIES

E. The oil refinery plant manager must calculate volume.

- F. A navigator uses parallel lines in plotting the course of his ship.
- E. The cylindrical oil tanks at a storage plant have a radius of 45 feet and a height of 110 feet. There are 35 of these tanks.

 (There are 7.5 gallons in 1 cubic foot.) What is the total capacity of the 35 tanks?
- F. A ship is located at point P near the East coast of the U.S. The captain wants to travel on a course parallel to the East coast. The navigator plots this course by constructing a line through P parallel to the coast. Make the necessary construction.



- 1. Draw any line through P that intersects line AB at point G.
- 2. From G, draw an arc that intersects lines PG and AB at F and K respectively.
- 3. Using the same compass setting from P draw an arc that intersects line PG and T.
- 4. Measure line segment FK.
 Set the compass at this measure.
- 5. From T using compass measure determined in step 4, draw an arc that intersects arc drawn in step 3, and label the point of intersection N.
- 6. Draw a line through points P and N.

- G. Congruence
 - 1. Segments
 - 2. Angles
 - 3. Triangles
 - 4. Other polygons
- H. Problem solving

- G. To demonstrate an understanding of congruence, the student should be able to determine by measurement or from given facts:
 - 1. Congruent segments.
 - 2. Congruent angles.
 - 3. Congruent\triangles.
 - 4. Congruent polygons.
- H. To extend the above concepts and skills the student should be able to solve problems about areas, volumes, and perimeters.



RELATED CAREER ORIENTED
LEARNING ACTIVITIES

- G. Surveyors can use congruence in determining distance.
- G. Use congruence of triangles to explain how the distance across a lake can be determined.

- H. People in different careers require different performance skills. However, computational ability is needed in every occupation.
- H. A concrete mason needed to calculate the cost of concrete for the following project:

 The cost of ready mix concrete is \$33.95 per cubic yard.

 Garage floor--20'x20'x4''

 Drive way--23'x30'x4''

 What is the total cost of the concrete?

Other problems encountered by people in different careers may be found in the text, supplementary texts, or drawn from problems encountered by businesses in the community.

0

PERFORMANCE OBJECTIVES

IV. Measurement

IV. Measurement

- A. Metric measurement
 - l. Basic units (using ''hands-on'' measuring ; instruments)
 - 2. Prefixes

- 3. Conversion from one metric unit to another
- 4. Problem Solving

- A. To demonstrate a basic understanding of metric measurement, the student should be able to:
 - 1. Use the basic metric units of length (meter) weight (gram), capacity (liter), and temperature (Celsius) in actual measuring activities with metric measuring instruments.
 - 2. Define the prefixes commonly used in the metric system:
 - a. Milli (m).
 - b. Centi (c).
 - c. Deci (d).
 - d. Deca (da).
 - e. Hecto (h).
 - f. Kilo (k).
 - 3. Convert measurements which are expressed in given metric units to measurements in other metric units.
 - 4. Use metric measurements to solve problems concerning:
 - a. Perimeters.
 - Areas.

RELATED CAREER ORIENTED LEARNING ACTIVITIES

IV. Career Concept

Careers require different knowledge, abilities, attitudes, and talents.

Performance Objectives

A. The metric system is used in international sports competition.

Therefore, an athlete should have a knowledge of the metric system.

The metric system is used in all scientific investigations. Therefore, a chemist must know the metric system.

A. Using a yard stick and a meter stick, determine which is longer. In the United States, track and field events include the 100-yard dash. In the Olympic games, the 100-meter dash is used. Which is longer?

Density = mass . Find unit volume
the density of cement, if a piece 2 cm × 2 cm × 9cm weighs 108g.
Answer---3g/cm³.

PERFORMANCE OBJECTIVES

B. English measurement

Comparison of metric and English units (using "hands on" measuring instruments)

D. Rounding and estimation

- B. To demonstrate a basic understanding of the English units of measurement, the student should be able to name the units and use the measuring devices in the actual measurement of objects.
- C. To demonstrate an understanding of the relationship between units of length, weight, capacity, and temperature in the two systems, the student should be able to measure given objects and materials, using measuring devices. He should record the measurements using units of both systems.
- D. To demonstrate a basic understanding of rounding and estimation, the student should be able to:
 - Give the number of significant digits in a given number.
 - 2. Round to a given number of digits.
 - 3. Estimate answers of given problems.

RELATED CAREER ORIENTED LEARNING ACTIVITIES

- B. The U.S. is the only major country which still uses the English system of measurement; for example, the auto industry, the clothing industry, the construction industry, etc.
- B. To review the English units, use actual measuring devices to measure weight, length, capacity, and temperature of given objects. Record the measurements.
- C. The consumer needs to develop concepts of the relations between the two systems.
- C. Measure the same objects using metric devices. Record the measurements on the same table used in "B" above. Notice how the units are related. Make a display of table and articles that express measurements in both systems.

- D. People who use measurements in their occupations are actually dealing with approximate numbers. They often round such numbers to a given number of significant digits.
- D. Tom, a pilot, uses . 9 gallons of gasoline for each mile flown by his plane. He had 34 7/8 gallons of gasoline. He wants to know approximately how far that much gasoline will take him. He uses rounding and estimates the distance he can travel. How would you estimate the distance?

- E. Scientific notation
- E. To demonstrate a basic understanding of scientific notation, the student should be able to:
 - 1. Convert a decimal number to a number expressed in scientific notation.
 - 2. Convert a number expressed in scientific notation to a decimal number.

RELATED CAREER ORIENTED LEARNING ACTIVITIES

- E. Physicists are often concerned with very large or very small numbers.
- E. The speed of light in a vacuum is 29,979,280;000 cm/sec.
 Use scientific notation to express the number.
 Answer: 2.997928 × 10¹⁰ cm/sec.

The distance from the earth to the sun is 93,005,000 miles. Use three significant figures and express the distance using scientific notation. Answer: 9.30×10^7 miles.

PERFORMANCE OBJECTIVES

V. Introduction to Statistics

V. Introduction to Statistics

A. Graphs

- 1. Bar
- 2. Line
- 3. Circle
- 4. Other
- B. Measures of central tendency
 - 1. Organization of data
 - 2. Analysis of data
 - a. Mean
 - b. Median
 - c. Mode
 - d. Range

- A. To demonstrate a knowledge of graphs, the student should be able to construct and interpret the following graphs:
 - 1. Bar.
 - 2. Line.
 - 3. Circle.
 - 4. Other.
- B. To demonstrate a basic understanding of measure of central tendency, the student should be able to:
 - 1. Organize given data using a frequency table.
 - 2. Analyze the given data by determining the:
 - a. Mean.
 - b. Median.
 - c. Mode.
 - d. Range.

RELATED CAREER ORIENTED LEARNING ACTIVITIES

V. Career Concept

Some occupations from different career clusters require the ability to statistically evaluate data.

Performance Objectives

- A. Many firms use graphs to show significant relationships between quanitities.
- A. Collect different types of graphs from newspapers, pamphlets, brochures, and magazines.

 Interpret the graphs. Make a bulletin board display using some of the graphs.

B. The guidance counselor organizes data gathered at the local level and compares them with state and national levels.

Use the data from the most recent test scores in class to make a frequency table. The following list shows the 10 scores on a recent test.

Joe	(7 9)	Yvonne	(77)
Milton	(80)	Myrtle	(80)
Louie	(75)	Margaret	(80)
Joycelyn	(75)	Sandra	(88)
John V	(82)	Ann	(81)



RELATED CAREER ORIENTED LEARNING ACTIVITIES

The statistician applies mathematics in market research and commercial sample surveys.

Complete the mean, the median, the mode, and the range.

Detergent	Units of Phosphates			
Calgon	75.5			
Axion	43.0			
Biz	40.4			
Salvo	30. 7			
Punch	25.8			
Ajax Laundry	25. 2			
Spic & Span	23. 0			
Breeze	22. 2			
Cheer	22.0			
Fab	21.5			
Cold Water All	9. 8			
Wisk	7. 6			
Trent	1.4			

Reserachers gather and organize data.

Gather some data about yourself and some of your friends. You may want to list your weights to the nearest pound, your height to the nearest inch, or your scores on the mathematics test. Make a frequency table from the data. Compute the range, the mode, the median, and the mean.

PERFORMANCE OBJECTIVES

VI. Enrichment Topics

VI. Enrichment Topics

- A. Other Numeration Systems
 - 1. Egyptian and Roman
 - 2. Base two and base five
 - 3. Table Construction
 - a. Addition, base
 2
 - b. Multiplication, base 2
 - c. Addition, base
 - d. Multiplication, base 5
 - 4. Identity elements in other bases for addition and multiplication

- 'A. To demonstrate a basic understanding of other numberation systems, the student should be able to:
 - Write a given list of numbers in Egyptian and Roman numerals.
 - 2. Express numbers in:
 - la. Base two.
 - b. Base five.
 - To construct tables:
 - a. Addition, base
 - b. Multiplication, base 2.
 - c. Addition, base
 - d. Multiplication, base 5.
 - 4. Identify the identity elements for addition and multiplication in the following systems:
 - a. Base two.
 - b. Base five.

RELATED CAREER ORIENTED LEARNING ACTIVITIES

VI. Career Concept

Individuals seek careers for various reasons.

Performance Objectives

A. Historians use both Egyptian and Roman numeration systems.

A.	Our Number Symbol	Egyptian Symbol	The Object
	1		A vertical stroke of staff
	10		A heel bone
	100 \$ 1,000	9 J	A coil or rope or scroll
	10,000	1	A bent finger
	100,000	∞	A burbot
⇒ 1	,000,000	13	An astonished man

Use the chart above to decode the numerals on the stones.



PERFORMANCE OBJECTIVES

5. Conversion

- 5. Convert:
 - a. A given number in the decimal system to its equivalent in base two.
 - b. A given number in base two to its equivalent in the decimal system.

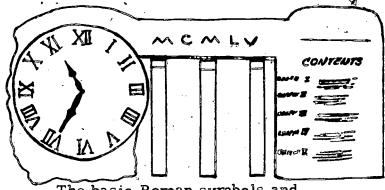
- B. Tests for divisibility
 - 1. By 10, 5, 2
 - 2. By 3, 9
 - 3. By 6

- B. To demonstrate an understanding of divisibility tests, the student should be able to determine the divisibility of any given number by:
 - 1. 10, 5, 2.
 - 2. 3, 9.
 - **b** 3. 6.



Y.

RELATED CAREER ORIENTED LEARNING ACTIVITIES



The basic Roman symbols and their values are shown below.

Ī.	V	X	L	С	D	M
ī	5	10	50	100	500	1000

Read the chapter numerals, the time on the clock, and the date on the building. Write these numerals in the Hindu-Arabic (decimal) system.

The devices in electronic computers are like electric lights in that each device has only two states, ON and OFF. This device can represent 1 by an ONstate and 0 by an OFF-state.

Using red dots for ON and black dots for OFF, show how the decimal number 6 is represented.

B. Conduct an informal interview of an accountant or a computer programmer to determine how he uses divisibility tests.

The modern electronic computer is based on the binary system (the base two system).

B. An accountant uses certain divisibility tests to check his calculations.



- 94. By 8
 - 5. Bv 4
- C. History of mathematics

- D. Probability
 - 1. Probability of an event
 - 2. Probability of two outcomes
 - a. With replacement
 - b. Without replacement

- 4. 8.
- 5. 4.
- C. To demonstrate a knowledge of the history of mathematics the student should be able to answer the teacher's questions on the historical facts taught in the class.
- D. To demonstrate an elementary understanding of probability and chance, the student should be able to:
 - l. Compute the probability of selecting a red checker from a box which contains 4 red checkers and 8 black checkers.
 - Compute the probability of drawing two blue marbles in succession from a box containing 4 red marbles, 3 white marbles, and 5 blue marbles, given the following condition:
 - a. Draw one marble.
 Replace it, then
 draw again.
 - Draw one marble.
 Do not replace it,
 then draw again.



RELATED CAREER ORIENTED LEARNING ACTIVITIES

- C. Mathematicians, teachers, and authors of mathematics texts are aware of significant historical facts and developments that have influenced mathematics.
- D. Pollsters, weathermen, health authorities, and others use probability. The life insurance actuary, using previously established statistical records and mathematical probability, determines life insurance rates.
- C. Collect reports, mathematical diagrams and pictures that illustrate historical developments in the history of mathematics, etc., for a bulletin board display. Conduct classroom demonstrations of how some measurements determined by the Greeks, Egyptians, and others may be made.
 - D. In a Louisiana city with a population of 19,560, the health authorities estimated that approximately 2,934 people will contact influenza during the winter.

 What is the probability that a resident will contact influenza?

- E. Squares and square roots
 - 1. Estimating and computing

- 2. Using the Algorithm
- 3. Using tables
- 4. Theorem of Pythagoras

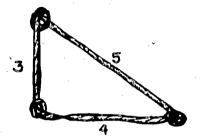
- E. To demonstrate a basic understanding of squares and square roots, the student should be able to:
 - 1. Write the squares of numbers from 1 to 20 and then use the information to compute square roots of given numbers less than 400 by the division and average method.
 - 2. Compute the square root of a given num; ber by use of the algorithm.
 - 3. Compute the square and square root of any given number using a table of squares and square roots.
 - 4. Compute the third side of a right triangle when the length of any two sides are given.



RELATED CAREER ORIENTED LEARNING ACTIVITIES

- E. Carpenters sometimes
 use squares and square
 roots in calculating
 lengths of braces for
 gates, supports for
 shelves, and lengths of
 rafters for houses
 when they work from
 sketches that give only
 part of the needed information.
- found that a triangle whose sides are 3 units, 4 units, and 5 units long would be a right triangle.

 Therefore, a knotted rope 12 units long could be used to lay out a square corner.



Sam wondered if a triangle whose sides were 4", 5", and 6" long would be a right triangle. He used the hypotenuse rule (Theorem of Pythagoras) to decide. He then substituted into the formula $a^2 + b^2 = c^2$. What should he discover?